GPR Monitoring of Volumetric Water Content in Soils Applied to Highway Construction and Maintenance

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1. Introduction

Detailed knowledge of the subsurface water content is important for highway design, maintenance, and repair. Transportation engineers can monitor the water content of sub-asphalt soils to estimate the soil stiffness as an index of the likely performance of a pavement and to evaluate the need for subsurface drainage retrofits. Conventional approaches for measuring water content include gravimetric sampling, time domain reflectometry [TDR], and neutron probes, all of which are time-consuming and invasive. Additionally, each of these methods provides only point measurements; since soil moisture content can vary greatly over space and time, point measurements are of limited value when surveying over a large area and over a period of time. An alternative to these conventional methods is ground penetrating radar (GPR), which can be used to quickly collect continuous, high-resolution water content estimates. GPR techniques can be used to estimate water content due to the sensitivity of electromagnetic velocity to water content. The two experiments described here, a controlled pit study and a transportation application in sub-asphalt soils, are based upon measuring the velocity of common-offset GPR reflections, which allows estimation of water content over deeper intervals than is possible with groundwave data and more quickly than can be accomplished with common-midpoint surveys. To estimate the velocity from GPR reflections, both the travel path and the travel time of the electromagnetic energy must be known. With commonoffset GPR techniques, the two-way travel time of the energy from the surface to the reflective interface and back is measured. To estimate electromagnetic velocity, the depth of the reflective interface must be determined. For engineered materials, the depth of a reflective layer might be known from construction records; for natural soils, calibration boreholes could be used to estimate the depth of soil layer interfaces.

After the electromagnetic velocity (v) has been calculated, it can be converted to the real part of the dielectric constant, κ , using the following relationship:

$$\kappa = \left(\frac{c}{v}\right)^2 \tag{1}$$

where c is the plane-wave propagation velocity of electromagnetic waves in free space (Davis and Annan, 1989). A petrophysical relationship can be used to convert κ to volumetric water content (θ_{ν}). One commonly used petrophysical relationship is a volumetric mixing model developed by Roth et al. (1990):

$$\theta_{v} = \frac{\kappa_{effective,mixing}^{1/2} - (1 - \eta)\kappa_{solid}^{1/2} - \eta\kappa_{air}^{1/2}}{\kappa_{water}^{1/2} - \kappa_{air}^{1/2}}$$
(2)

where η is porosity, κ_{air} , κ_{solid} , and κ_{water} are the dielectric constants of the air, solid, and water components of the mixture, respectively, and $\kappa_{effective,mixing}$ is the estimate of dielectric constant obtained from electromagnetic measurements. For increased accuracy, site-specific relationships can also be developed.

2. Water Content Estimation in Sandy Test Pits

2.1. Construction of Test Pits

To determine the accuracy of common-offset GPR for providing estimates of water content, three test pits filled with sandy soil having carefully controlled water contents were constructed. During construction, reflectors were buried at measured depths throughout the pits. The first pit had sides 3m in length, was 1.5m deep, and had an average θ_v of 0.20. The other two pits had sides 2m in length and were 0.8m deep; one of these pits had a θ_v of 0.06 and the other was 0.12. Test pits were employed instead of natural soil deposits to enable control of the water content and to ensure homogeneity of the soil throughout the test volume. Under these conditions, the variations in κ obtained from GPR reflection data could be investigated solely as a function of θ_v . A well-sorted, silty sand was chosen as the test soil, since this soil type is optimal for GPR signal penetration and is similar in composition to the sub-asphalt materials used in the transportation industry. The depths of the pits were chosen based on the requirements for water content measurements transportation applications, and the lateral dimensions were designed to allow several reflectors to be buried in the pit sufficiently far apart as to avoid reflection interference between buried reflectors and the walls of the pit.

The soil was placed in the pits and compacted in successive layers of 10 to 15cm in thickness. After compacting each layer, two to four soil samples of approximately 600g each were taken from different locations on

the layer surface, and the gravimetric water content (θ_g) was calculated for each sample. Two density measurements were also taken after the compaction of each layer using a Portaprobe Model B ® Mark II nuclear density gauge. For each soil sample, θ_v was calculated by multiplying θ_g by the soil density. These measurements showed that θ_v did not vary laterally across each layer in any of the pits, though these values did vary somewhat vertically from one layer to another in the pit with 0.20 θ_v . Figure 1 shows the calculated profile of θ_v in each pit from these data. In addition to these measurements, neutron probe access tubes were also installed in the pits to monitor the distribution of θ_v with time.

Several different types of reflectors were buried in the test pits to determine which produced the clearest and most easily interpretable reflections. The buried reflectors included solid aluminum plates (25cm on each side and 1cm thick), segments of hollow steel and aluminum pipes (21cm long, 11cm in diameter, with walls 0.5cm thick), and hollow PVC plates filled with water (PVC sheets 18cm on each side and 0.25cm thick, with 2cm of water between the upper and lower sheets). The reflectors were buried during layer compaction at depths ranging from 11 to 120 cm below the pit surface, and different configurations of reflectors were tried. Most reflectors were simply buried in the pit, but some reflectors were 'stacked', or buried over another reflector, with a vertical distance of at least 18cm between each reflector. The locations of the reflectors and the access tubes for the pit with 0.20 θ_{ν} are shown in map view in Figure 2. The location and elevation of each reflector were accurately surveyed during construction of the pits.

2.2. Data Collection

After the test pits were completed, geophysical surveys were performed using surface GPR and neutron probe measurements. The GPR surveys were collected along several traverses across each pit; each traverse passed over two or more of the buried reflectors, as illustrated in Figure 2. GPR measurements were taken using four central frequencies: 225, 450, 900, and 1200 MHz, with a 1cm station spacing for all frequencies. The GPR surveys showed very clear responses from the buried reflectors at all frequencies; the reflections arrived in a hyperbolic pattern as the GPR apparatus was pulled over the reflectors. Figure 3 shows reflections collected at a central frequency of 450 MHz in the pit with $0.20 \,\theta_{\nu}$ from two aluminum plate reflectors buried at depths of $0.60 \,\mathrm{m}$ and $0.85 \,\mathrm{m}$ below ground surface [BGS].

Neutron probe data were collected at a downhole sampling interval of 5cm coincidentally with the surface GPR surveys. Neutron probe data are measured in "backscattered counts", which can be related to water content. The neutron probe measurements in each pit were very similar in all of the access tubes at each depth, which supports the lateral uniformity of water content shown in the θ_g measurements (Figure 1).

After the geophysical measurements were completed, the pits were excavated, and additional θ_g measurements were taken at various depths. These measurements were compared to those taken during pit construction. From the similarity of the θ_g measurements before and after the geophysical surveys, the θ distribution in each pit was determined to be constant with time.

2.3. Estimation of Water Content from Surface GPR Measurements

The θ_{ν} in each pit was estimated by calculating the electromagnetic velocity between the surface and the buried reflectors and also between the 'stacked' buried reflectors. The velocity from the surface to the buried reflectors was calculated by measuring the travel time from the air wave, corrected for onset delay, to the apex of the reflection hyperbola. This travel time is the interval in which energy travels vertically from the ground surface to the buried reflector and back, and it occurs when the GPR apparatus is directly over the center of the reflector. Using this travel time (Δt_0 in Figure 3) and the known depth to the reflector, the velocity can be calculated, and κ can be determined using equation (1). This κ is an average value for the vertical interval between the surface and the buried plate. The velocity over the interval between stacked reflectors was calculated in a similar manner, by taking the difference in travel times between the two hyperbola peaks. This method reduces the uncertainty inherent in picking the absolute 'zero time' from the air wave and allows calculation of κ over smaller vertical intervals.

After κ was determined for each depth interval, both soil-specific and published petrophysical relationships were used to estimate θ_{ν} . The soil-specific relationship was developed using laboratory measurements of κ collected with a Trase Model 6050X1 TDR apparatus with 15cm waveguides and corresponding θ_{ν} measurements. By fitting a curve through this data, the following soil-specific petrophysical relationship was created:

$$\theta_{y} = -0.0006\kappa^{2} + 0.294\kappa - 0.092. \tag{3}$$

Figure 4 shows the comparison of the θ_{ν} estimates derived from GPR data using equations (2) and (3) with the θ_{ν} measurements obtained gravimetrically. The gravimetrically-derived θ_{ν} values were arithmetically averaged over the vertical intervals in which the electromagnetic velocity was measured for comparison with the GPR estimates. Two GPR-obtained estimates are shown for each gravimetrically-obtained θ_{ν} measurement; each GPR estimate is from a different traverse, and two traverses were taken over each reflector. Using the volumetric mixing model (equation (2)) with a measured average porosity of 0.26 and κ_{solid} of 6.3, the average absolute difference between the measured and estimated θ_{ν} in the test pits was less than 0.012. Using the soil-specific petrophysical relationship (equation (3)), the average absolute difference was less than 0.008.

The accuracy of the GPR estimates did not appear to be influenced by θ_{ν} , but it was affected by the geometry of the buried reflectors. The 'stacked' reflectors gave the most accurate θ_{ν} estimates, while the estimates over the intervals from the ground surface to a reflector were slightly less accurate. This result is likely due to uncertainty in the exact time that the GPR signal enters the ground; this inaccuracy does not affect between-reflector estimates. All reflector types gave clear reflections, but certain configurations were easier to interpret. The stacked reflectors were most efficient if the overlying reflector was thin (e.g., an aluminum plate) and did not generate reflections from both the top and bottom of the reflector. Reflectors that were placed at least 20cm below the ground surface were also easier to interpret, as the ground wave did not interfere with reflected arrivals at this depth.

In addition to the reflector geometry, errors in the GPR estimates of θ_{ν} could also be produced from uncertainties associated with picking the air and reflected waves, digitization of the GPR data, the petrophysical relationship invoked, and the depth measurement of the reflector. Although error due to picking the air and reflected waves is difficult to quantify, error analysis was performed to investigate the influence of the other factors. This analysis showed that the greatest cause for error was inaccurate depth measurements, with shallow reflectors having proportionately higher errors. The maximum and minimum θ_{ν} errors predicted were 0.048 and 0.003, which corresponded to the shallowest and deepest reflectors, respectively. Comparison of the GPR-obtained estimates of θ_{ν} with the gravimetrically-obtained measurements (Figure 4) illustrates that the GPR estimates are within the bounds suggested by error propagation analysis, and the measured error is usually considerably less than

that predicted by this analysis. Increased error is observed at the shallowest reflectors, which demonstrates that the intervals over which θ_v are estimated must be sufficiently thick so that small errors in depth estimation do not cause large errors in estimating θ_v .

3. Water Content Estimation in Sub-asphalt Soils

Based upon the success of using common-offset GPR for θ_v estimation in the sandy test pits, we applied this technique to the engineering application of monitoring θ_v in sub-asphalt aggregate soils. In this experiment, GPR surveys were collected in a grid over two differently designed pavement sections. The sections differed by the composition and thickness of the sub-asphalt aggregate layers and by the presence of a drainage layer in one of the sections. For both sections, water was injected into the aggregate layers, and additional GPR time-lapse surveys were collected over a period of several months. Finally, both sections were subjected to dynamic loading to simulate trafficking, followed by GPR data acquisition. Analysis of the GPR signal travel time through the aggregate layers prior and subsequent to both infiltration and loading allows estimation of the changes in θ_v with space and time due to natural drainage and dynamic loading. This information can be used to compare differently designed pavements and to correlate θ_v estimates with traditional pavement strength measurements. The following discussion, which is a summary of a single experiment conducted in one of the pavement sections prior to loading, demonstrates a practical application of GPR technology for obtaining θ_v estimates.

3.1. Site Description and Data Collection

The pavement section for this experiment was constructed by a contractor according to typical California Department of Transportation standards. The pavement was composed of four layers: asphalt rubber overlay, asphalt concrete (AC), aggregate base (AB), and aggregate sub-base (ASB), as shown in Figure 5. The rubber overlay and asphalt concrete have very low permeability and do not accumulate a significant amount of water, so this experiment focused on monitoring θ_{ν} in the aggregate layers. The upper aggregate layer, the AB, is heavily compacted and is composed of medium to coarse gravel in a matrix of silt and clay; the fines account for approximately 10% (by weight) of the AB. The ASB is similar to the AB in composition, but has a slightly higher percentage of fines and is not compacted. The ASB is the lowermost engineered layer; the soil below it is the subgrade (SG), which at this site is a highly plastic deltaic clay. The pavement section is located inside a hangar,

so the influences of the outside environment on θ_{ν} should be negligible.

Water was introduced into the sub-asphalt aggregate layers by means of a drip infiltration system. Infiltration holes were drilled upgradient of the pavement test section through the rubber overlay and asphalt concrete at 0.5m intervals for a length of 12m; the infiltration holes are shown as red circles in Figure 6. Water was injected into these holes four times a day for a total injection of 3 gal/day over the 12m zone; injection continued for a period of eight months. GPR data were collected over the test pavement at central frequencies of 900 and 1200 MHz prior to infiltration and periodically during the infiltration period. GPR traverses were collected using a 2cm station spacing along the grid indicated by blue arrows in Figure 6. The data collected at 1200 MHz along one GPR traverse is shown adjacent to the pavement cross-section in Figure 5. After the infiltration experiment was completed, eight 15cm boreholes were drilled, and samples of θ_g were collected over the full thickness of the aggregate layers. These samples were converted to θ_v using the density of the aggregate layers given in construction records for subsequent comparison with the GPR-obtained estimates.

3.2. Estimates of Water Content in Sub-asphalt Layers

The θ_{ν} in the sub-asphalt aggregate layers was estimated by measuring the travel time of the GPR signal through each layer, then calculating the velocity using the travel time and the known thickness of each layer. The velocity was converted to θ_{ν} using a soil-specific petrophysical relationship developed in the laboratory using TDR. The estimates of θ_{ν} obtained using this technique were compared to those obtained from gravimetric sampling and were found to agree well: the θ_{ν} estimates from GPR data varied from those obtained gravimetrically by a maximum of 0.025 in the AB and 0.027 in the ASB, and the average absolute difference between the GPR estimates and gravimetric measurements of θ_{ν} for the AB and ASB were 0.008 and 0.011, respectively. One cause of error in the GPR-obtained estimates of θ_{ν} was variations in the thicknesses of the aggregate layers that were not accounted for in the velocity calculations. Even with these errors, the GPR estimates of θ_{ν} were accurate enough to be useful for pavement applications. The 1200 MHz GPR data had the highest resolution and gave the best correlation with gravimetrically-obtained θ_{ν} measurements (R = 0.83); the results presented here are from the 1200 MHz data.

Using estimates of θ_v obtained from the GPR survey grid, the θ_v distribution in the sub-asphalt aggregate

layers was estimated over space and time. By observing changes in the θ_{ν} distribution with time, some of the hydrological properties of the aggregates can also be estimated. One method of observing changes in θ_{ν} is to calculate the change in θ_{ν} at each point between the post-infiltration survey and the pre-infiltration (dry) survey. Figure 6 shows the changes in θ_{ν} for the AB and ASB at 119 and 205 days after infiltration began. Negative changes indicate drying and are shown by yellow areas, while positive changes indicate water accumulation and are shown as blue areas. By identifying zones of wetting and drying in both aggregate layers, both vertical and horizontal flow paths can be inferred. In Figure 6, most of the water accumulation occurs in the ASB below the infiltration zone; this indicates that water may be flowing through vertically-inclined channels or flow paths in the lower permeability (higher compaction) AB and may be flowing more horizontally or being stored in the more permeable ASB. Localized areas of drying in the AB underlain by wetter zones in the ASB also support this hypothesis.

6. Conclusions

The experiments in the test pits and the pavement section show that common-offset GPR reflection data can be used to estimate θ_{ν} to a high degree of accuracy. The methodology developed in these two experiments provides a technique for obtaining quick, non-invasive, accurate, and high-resolution estimates of θ_{ν} . This method is applicable at sites where the layer thickness (or depth to the reflector) can be estimated with sufficient accuracy and in areas where GPR performs well, such as in low loss materials. This common-offset GPR technique could provide a valuable addition to current θ_{ν} estimation techniques under both engineered and natural conditions, and could be applied to various other subsurface applications in agriculture, ecology, and hydrology.

Acknowledgements: This study was funded by a grant from Caltrans, USDA 2001-35102-09866, and NSF EAR-0087802 to Yoram Rubin. We sincerely thank John Harvey and Michael Riemer for their unfailing support and advice throughout the experiments, and Ed Diaz and staff for their assistance with data collection.

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Figure Captions

Figure 1: Measured water content with depth in the three test pits. Two or more measurements were collected at different horizontal locations for each depth.

Figure 2: Map view of the pit with $0.20 \theta_v$ showing the surface location of the buried reflectors, surface GPR lines, and neutron probe access tubes. The reflectors in this pit were aluminum plates, each buried at a different depth.

Figure 3: Common-offset data collected over the pit with 0.20 θ_{ν} , along the traverse labeled "Line 2" on Figure 2.

Figure 4: Comparison of GPR-derived estimates of θ_{ν} with θ_{ν} measurements obtained gravimetrically from all three test pits. Equations (2) and (3) produced estimates very similar to the gravimetric measurements, suggesting that common-offset GPR can be used as a reliable water content estimation tool.

Figure 5: Vertical cross-section of the test pavement illustrating the thickness of the rubber overlay, asphalt concrete (AC), aggregate base (AB), aggregate sub-base (ASB), and subgrade (SG) and a 1200 MHz common-offset GPR survey line over this pavement showing the interpreted reflections from each interface. The water infiltration hole penetrates through the rubber overlay and AC and allows water to drip directly onto the AB.

Figure 6: Maps of the changes in water content observed at days 119 and 205 relative to pre-infiltration conditions in the AB and ASB. The contour maps are kriged interpolations from data collected along the surface GPR traverses shown as blue arrows. The blue and yellow areas on the contour maps represent zones of wetting and drying, respectively.

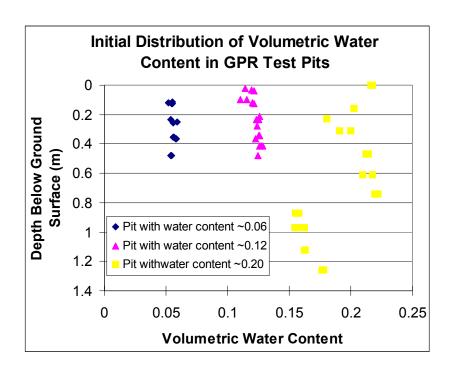


Figure 1

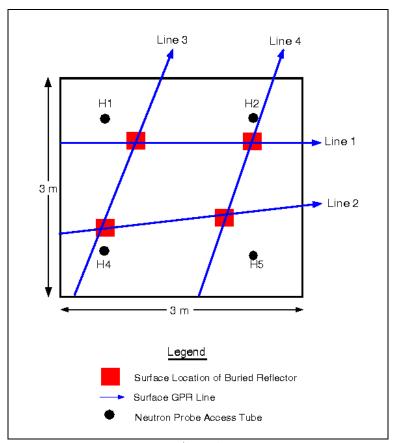


Figure 2

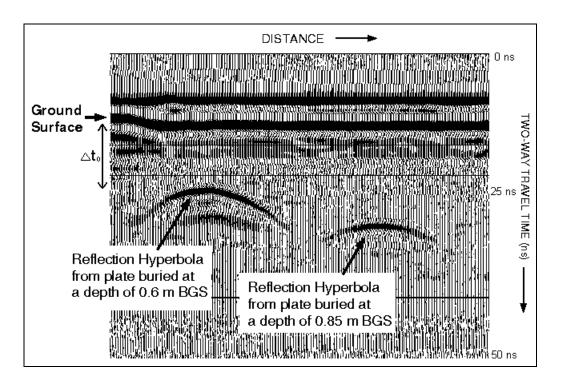


Figure 3

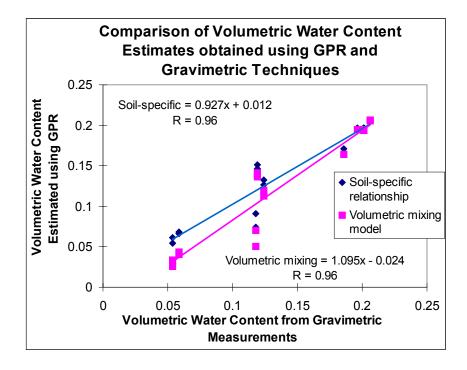


Figure 4

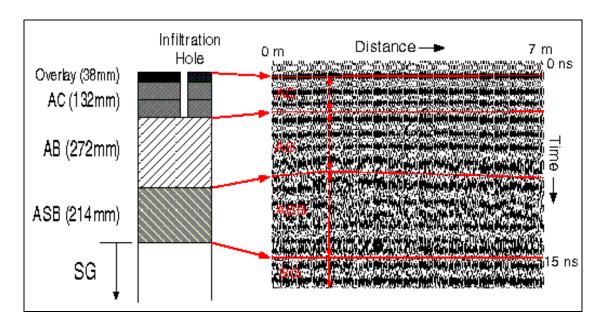


Figure 5

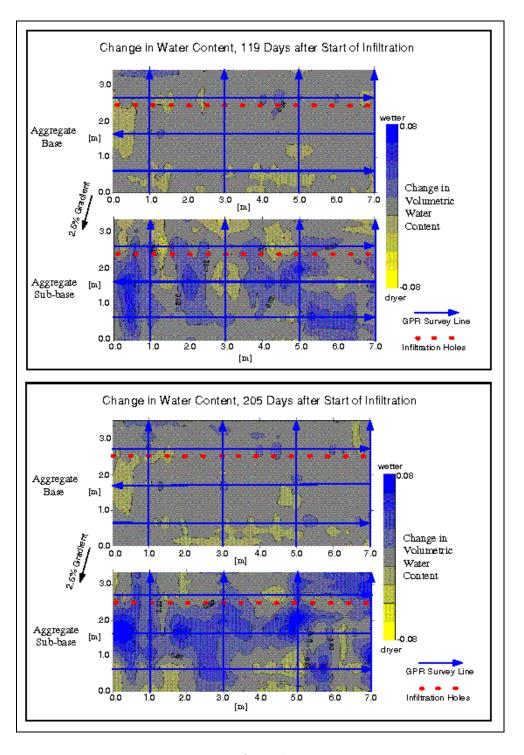


Figure 6